

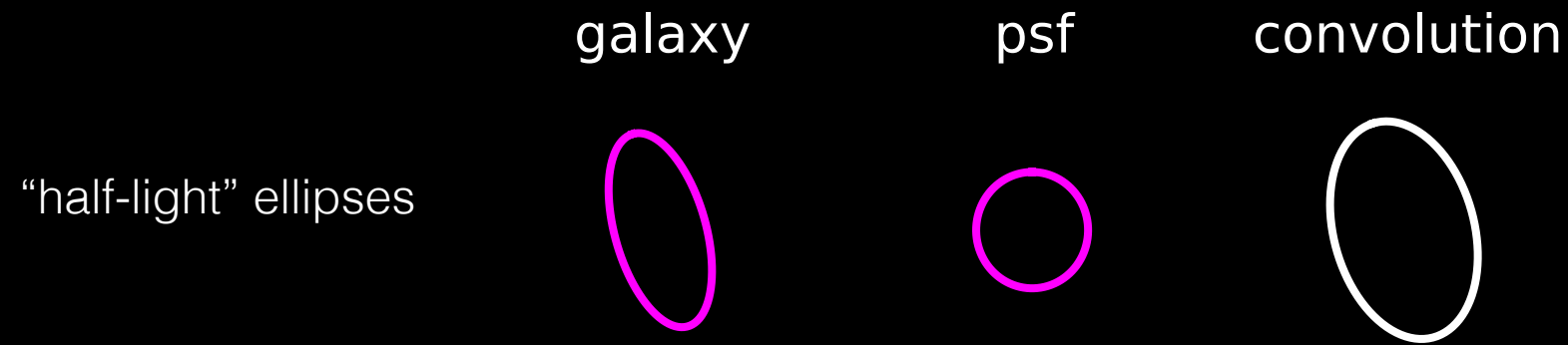
Impact of chromatic effects on galaxy shape measurements



Josh Meyers
Pat Burchat

PSF misestimation

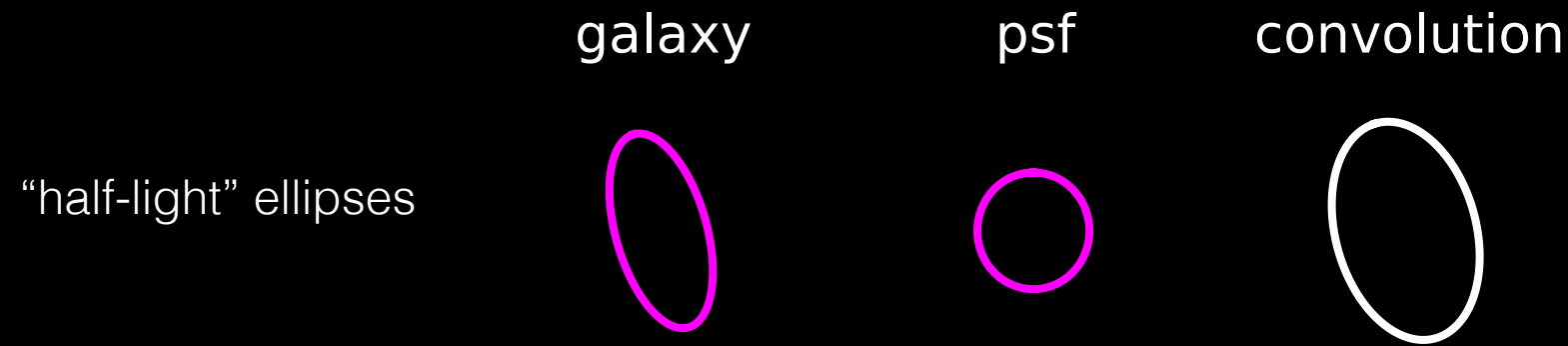
True galaxy gets convolved with PSF;
makes observed galaxy shape bigger and (generally) rounder.



Lensing pipelines attempt to invert this transformation.

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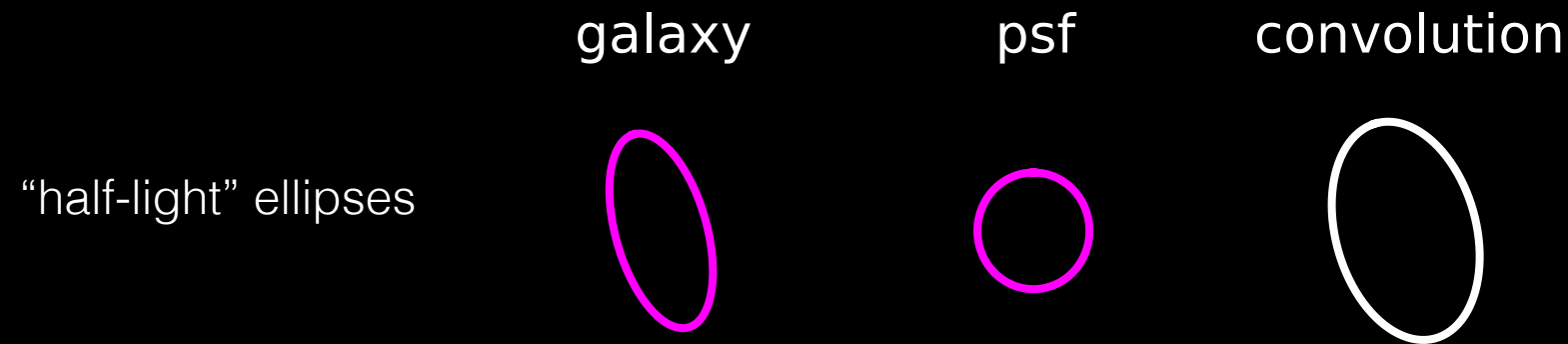


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Misestimating PSF size or shape leads to biased galaxy shape inferences.

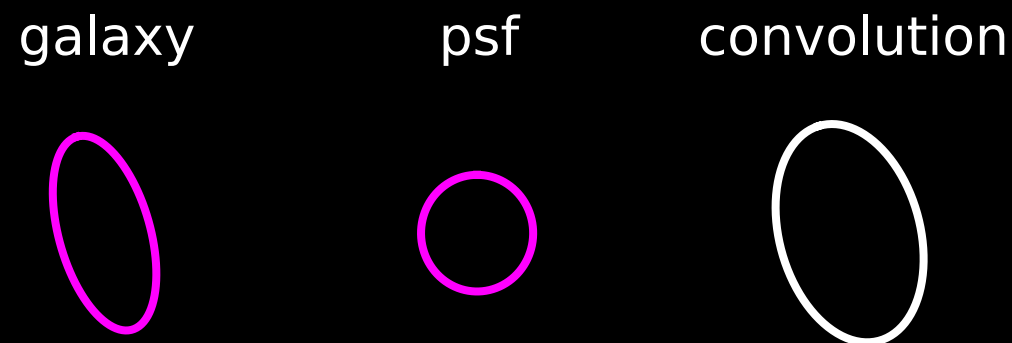
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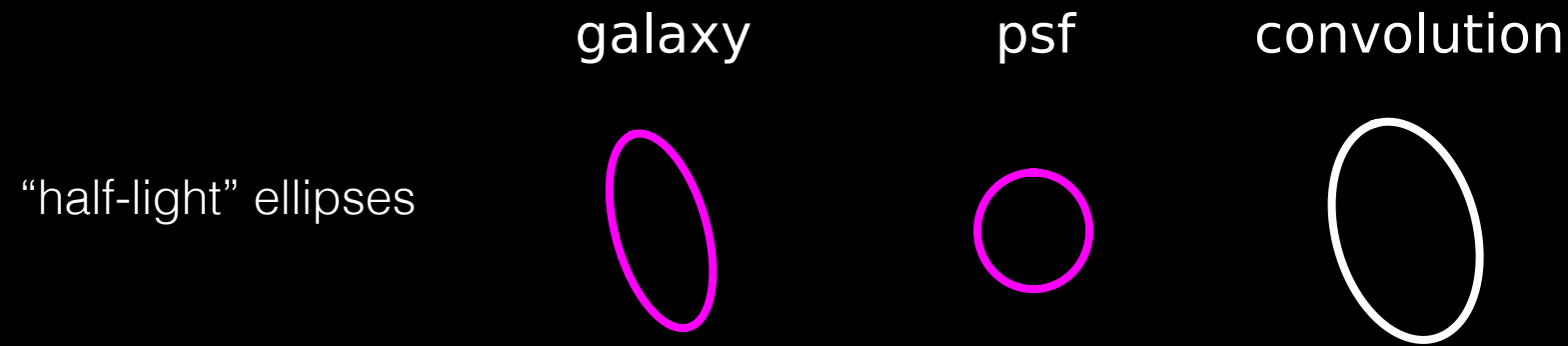
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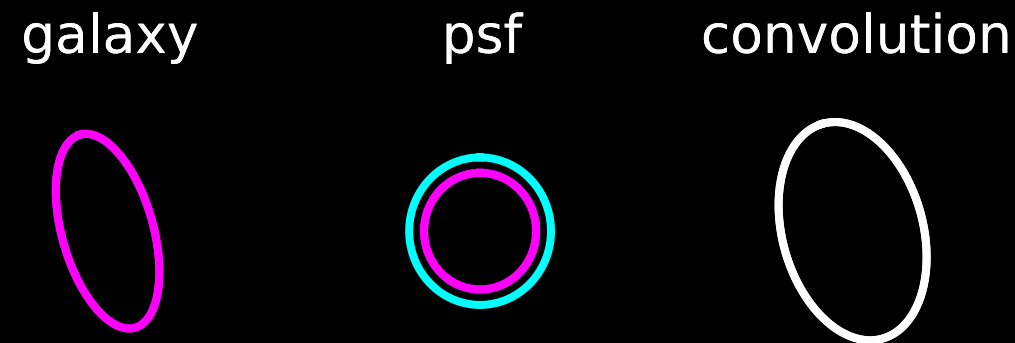
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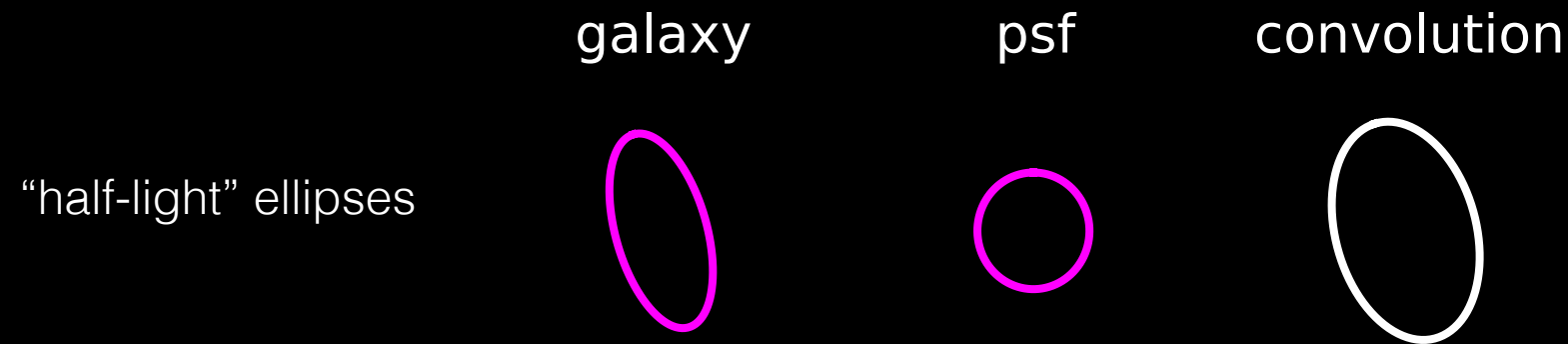
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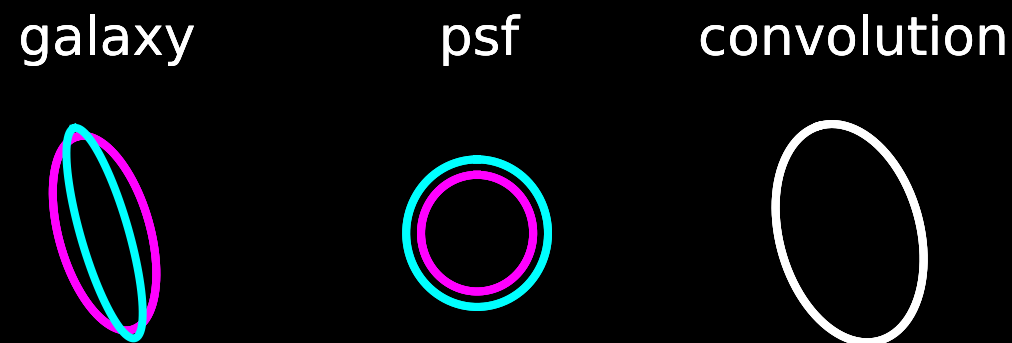
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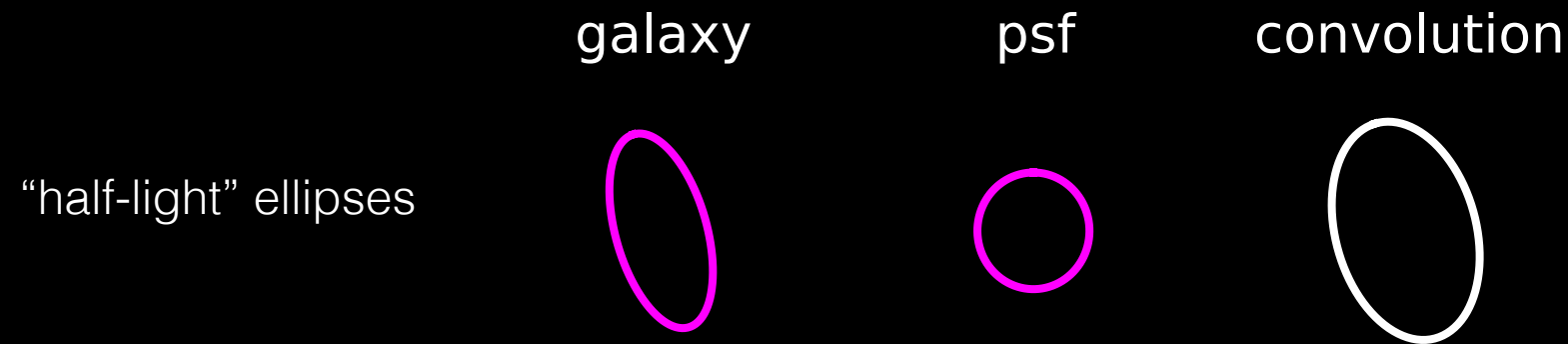
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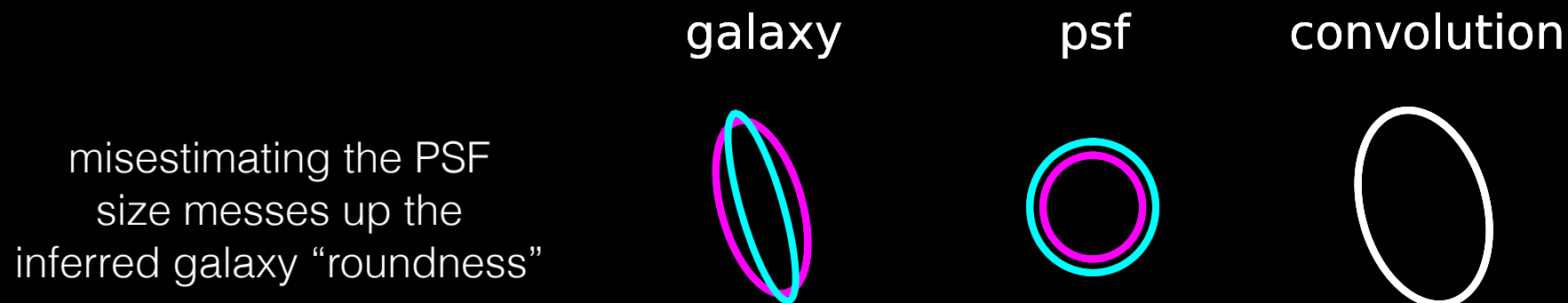
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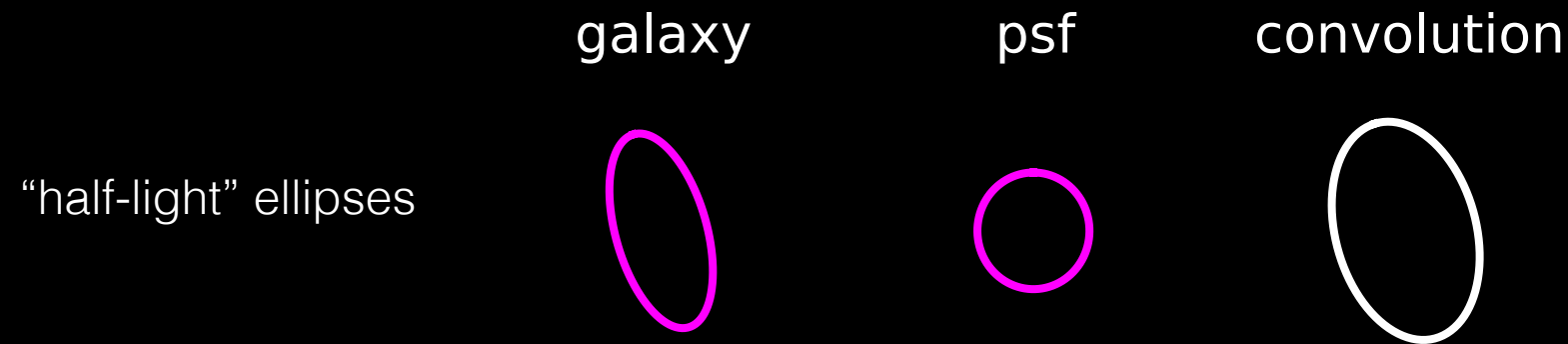
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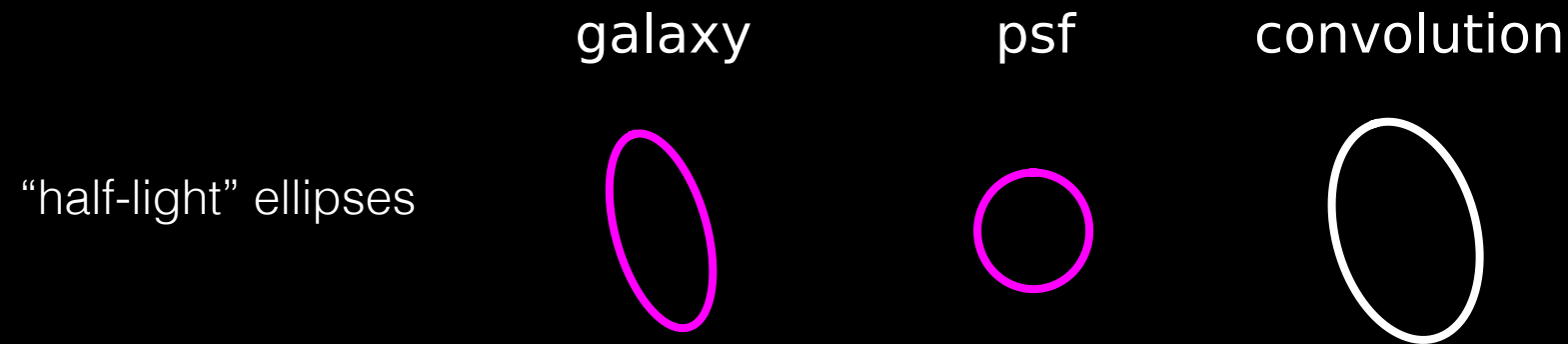
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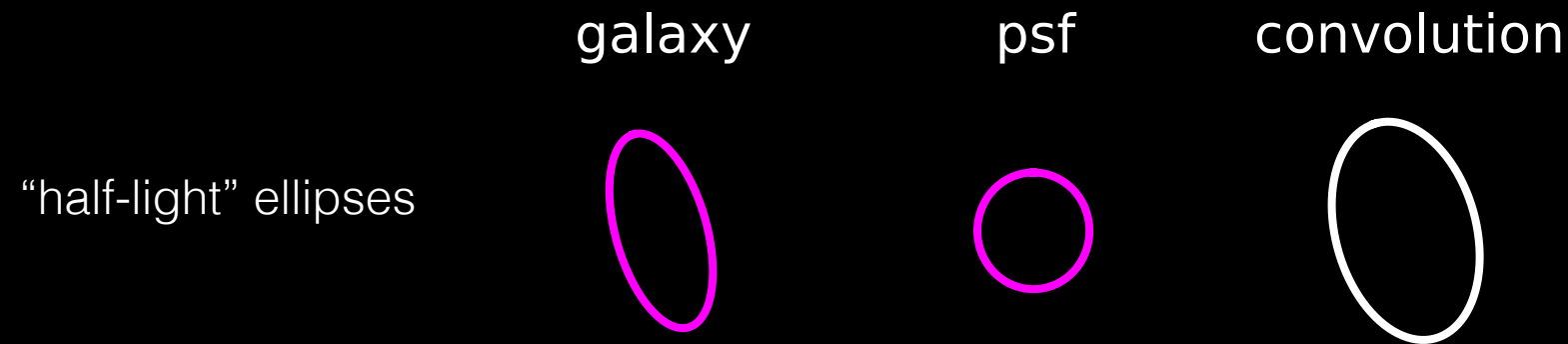
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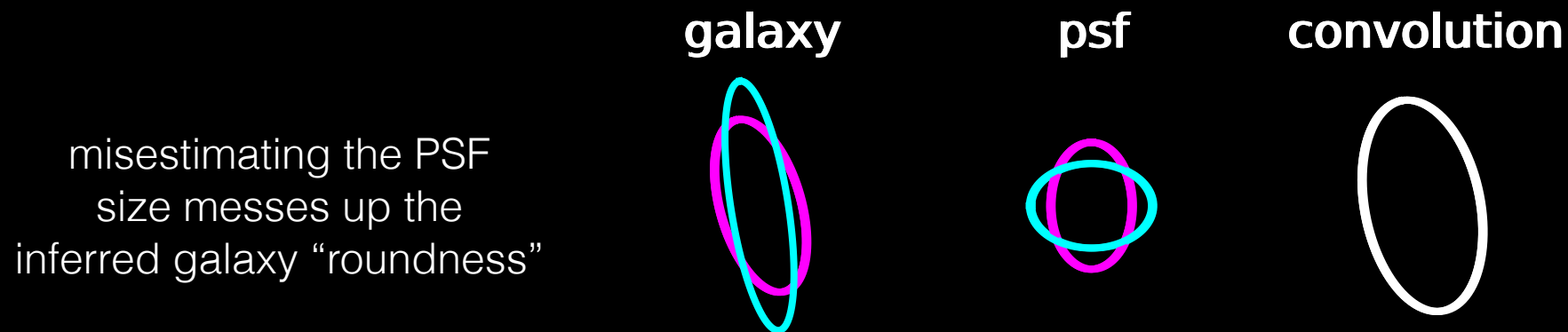
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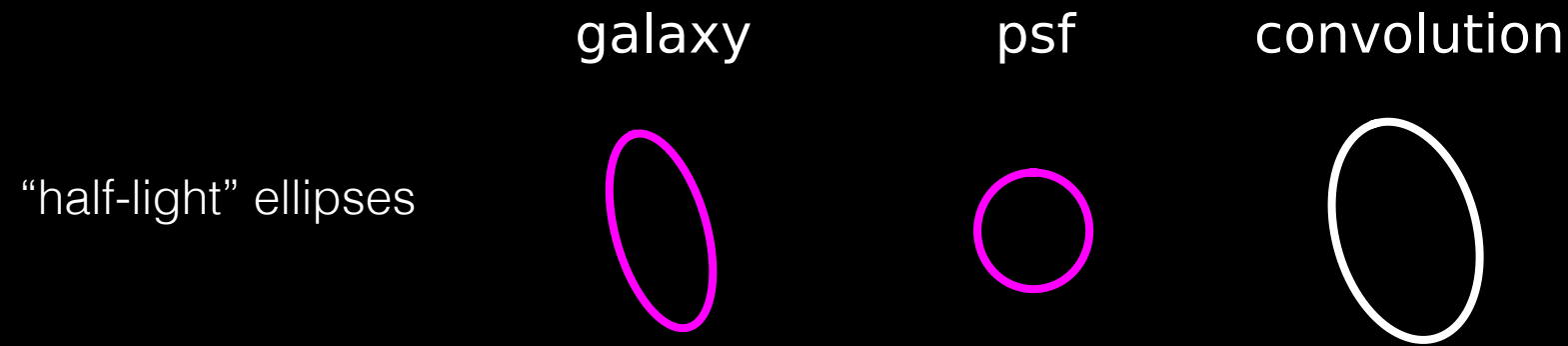
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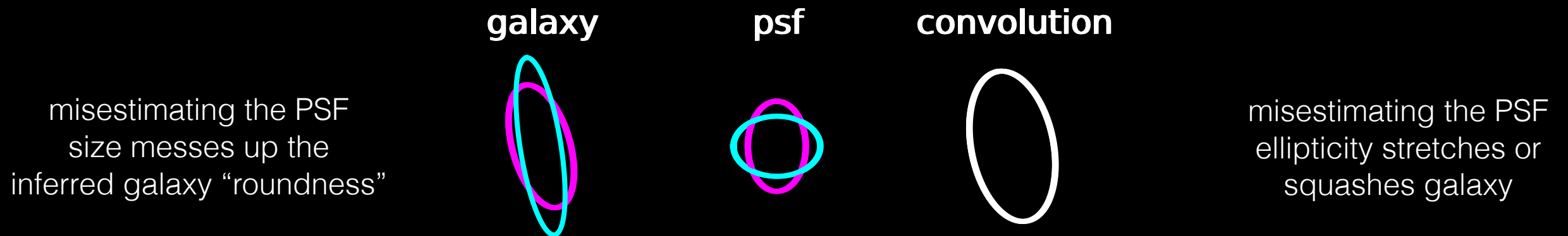
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PSF parameter definitions

Second moments:
$$I_{\mu\nu} = \frac{1}{\text{flux}} \int I(x, y) (\mu - \bar{\mu})(\nu - \bar{\nu}) \, dx \, dy$$

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$$\epsilon_1 = \frac{I_{xx} - I_{yy}}{I_{xx} + I_{yy}} \qquad \epsilon_2 = \frac{2I_{xy}}{I_{xx} + I_{yy}}$$

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Second-moment squared radius:
$$r^2 = I_{xx} + I_{yy}$$

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From ellipticity to shear:
$$\langle \epsilon \rangle \approx 2\gamma$$

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From ellipticity to shear:
$$\langle \epsilon \rangle \approx 2\gamma$$

Characterizing shear biases:
$$\hat{\gamma}_i = \gamma_i(1 + m_i) + c_i$$

PSF misestimation

Second moments add under convolution:

$$I^{\text{obs}} = I^{\text{gal}} + I^{\text{psf}}$$

galaxy



psf



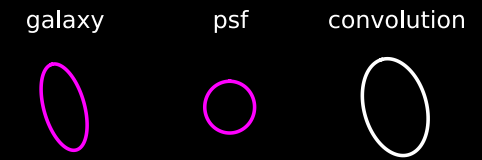
convolution



PSF misestimation

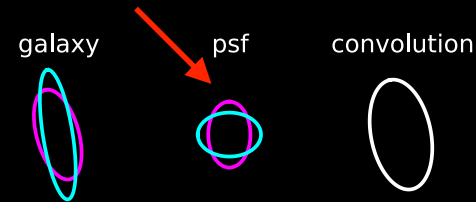
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PSF misestimate

$$\Delta I^{\text{psf}} = I^{\text{psf},*} - I^{\text{psf},g}$$



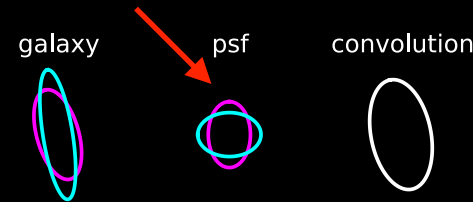
PSF misestimation

Second moments add under convolution:

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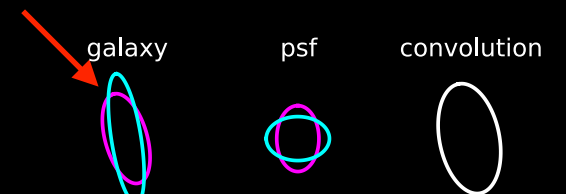

PSF misestimate

$$\Delta I^{\text{psf}} = I^{\text{psf},*} - I^{\text{psf},g}$$



Propagate into ellipticity

$$\epsilon_1 \rightarrow \frac{(I_{xx}^{\text{gal}} + \Delta I_{xx}^{\text{psf}}) - (I_{yy}^{\text{gal}} + \Delta I_{yy}^{\text{psf}})}{(I_{xx}^{\text{gal}} + \Delta I_{xx}^{\text{psf}}) + (I_{yy}^{\text{gal}} + \Delta I_{yy}^{\text{psf}})}$$

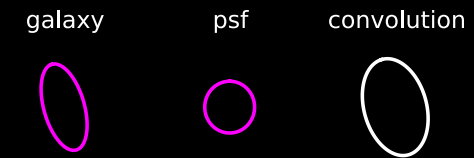


$$\epsilon_2 \rightarrow \frac{2(I_{xy}^{\text{gal}} + \Delta I_{xy}^{\text{psf}})}{(I_{xx}^{\text{gal}} + \Delta I_{xx}^{\text{psf}}) + (I_{yy}^{\text{gal}} + \Delta I_{yy}^{\text{psf}})}$$

PSF misestimation

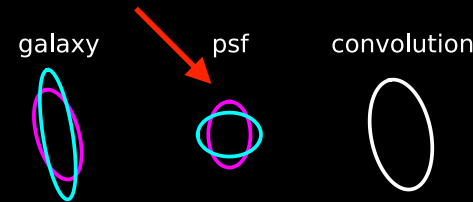
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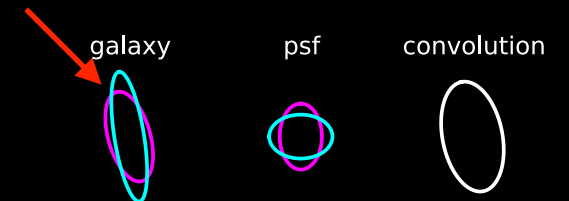
$$\Delta I^{\text{psf}} = I^{\text{psf},*} - I^{\text{psf},g}$$



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Algebra

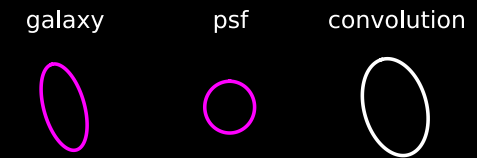
$$\epsilon_1 \rightarrow \epsilon_1 \left(1 - \frac{\Delta I_{xx}^{\text{psf}} + \Delta I_{yy}^{\text{psf}}}{r_{\text{gal}}^2} \right) + \frac{\Delta I_{xx}^{\text{psf}} - \Delta I_{yy}^{\text{psf}}}{r_{\text{gal}}^2} + \mathcal{O}(\Delta I)^2$$

$$\epsilon_2 \rightarrow \epsilon_2 \left(1 - \frac{\Delta I_{xx}^{\text{psf}} + \Delta I_{yy}^{\text{psf}}}{r_{\text{gal}}^2} \right) + \frac{2\Delta I_{xy}^{\text{psf}}}{r_{\text{gal}}^2} + \mathcal{O}(\Delta I)^2$$

PSF misestimation

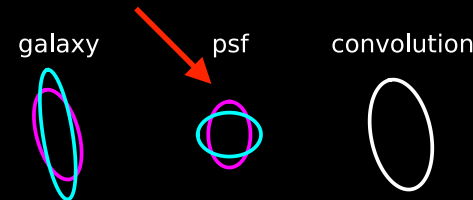
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PSF misestimate

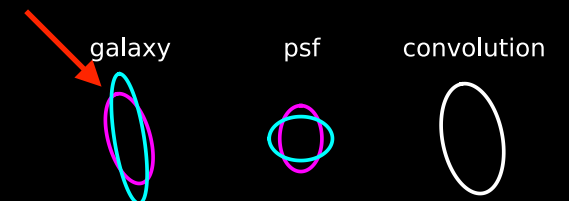
$$\Delta I^{\text{psf}} = I^{\text{psf},*} - I^{\text{psf},g}$$



Propagate into ellipticity

$$\epsilon_1 \rightarrow \frac{(I_{xx}^{\text{gal}} + \Delta I_{xx}^{\text{psf}}) - (I_{yy}^{\text{gal}} + \Delta I_{yy}^{\text{psf}})}{(I_{xx}^{\text{gal}} + \Delta I_{xx}^{\text{psf}}) + (I_{yy}^{\text{gal}} + \Delta I_{yy}^{\text{psf}})}$$

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Algebra

$$\epsilon_1 \rightarrow \epsilon_1 \left(\underbrace{1 - \frac{\Delta I_{xx}^{\text{psf}} + \Delta I_{yy}^{\text{psf}}}{r_{\text{gal}}^2}}_{\mathbf{m}} + \underbrace{\frac{\Delta I_{xx}^{\text{psf}} - \Delta I_{yy}^{\text{psf}}}{r_{\text{gal}}^2}}_{\mathbf{2c}} + \mathcal{O}(\Delta I)^2 \right)$$

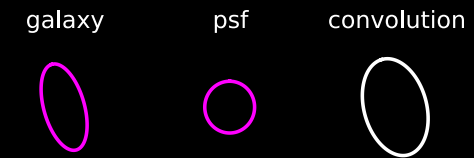
$$\epsilon_2 \rightarrow \epsilon_2 \left(\underbrace{1 - \frac{\Delta I_{xx}^{\text{psf}} + \Delta I_{yy}^{\text{psf}}}{r_{\text{gal}}^2}}_{\mathbf{m}} + \underbrace{\frac{2\Delta I_{xy}^{\text{psf}}}{r_{\text{gal}}^2}}_{\mathbf{2c}} + \mathcal{O}(\Delta I)^2 \right)$$

$$\hat{\gamma}_i = \gamma_i(1 + m_i) + c_i$$

PSF misestimation

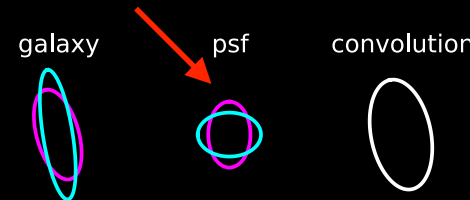
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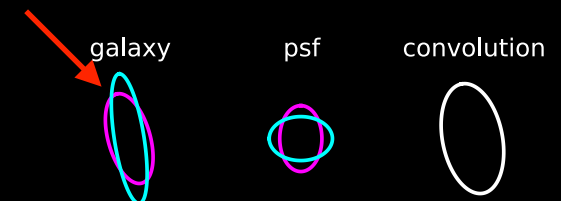
$$\Delta I^{\text{psf}} = I^{\text{psf},*} - I^{\text{psf},g}$$



Propagate into ellipticity

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$$\epsilon_2 \rightarrow \frac{2(I_{xy}^{\text{gal}} + \Delta I_{xy}^{\text{psf}})}{(I_{xx}^{\text{gal}} + \Delta I_{xx}^{\text{psf}}) + (I_{yy}^{\text{gal}} + \Delta I_{yy}^{\text{psf}})}$$



Algebra

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$$\hat{\gamma}_i = \gamma_i(1 + m_i) + c_i$$

generic, but assumes
unweighted second moments

Some sources of PSF misestimation

- Chromatic effects
 - PSF depends on wavelength
 - Measure PSFs from stars with stellar SEDs.
 - But! PSF affecting galaxy is derived from a galactic SED.

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 - Measure PSFs from stars with stellar SEDs.
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(same math is relevant for non chromatic effects too!)

- tree-rings
- chip edge effects
- brighter-fatter

Example: brighter fatter effect

- For LSST:
 - $r_{\text{gal}}^2 \sim (0.3 \text{ arcsec})^2 = 0.09 \text{ arcsec}^2$
 - $I_{\text{xx}}^{\text{PSF}} \sim 0.12 \text{ arcsec}^2 \Rightarrow \Delta I_{\text{xx}}^{\text{PSF}} \sim 0.0012 \text{ arcsec}^2$
 - $\Rightarrow m \sim 0.027$
 - compare to $m_{\text{req}} \sim 0.003$

Toy model for chromatic CCD PSF effects

Let CCD be chromatic,
but fix atmosphere and telescope to be achromatic.
(not realistic, but useful for isolating CCD effects).

$$I_{\mu\nu}^{\text{PSF}}(\lambda) = I_{\mu\nu}^{\text{PSF,telescope+atm}} + I_{\mu\nu}^{\text{PSF,CCD}}(\lambda)$$

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Moffat w/ FWHM ~0.65 arcsec

$$I_{\text{xx}} \sim 0.12 \text{ arcsec}^2$$

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Moffat w/ FWHM ~0.65 arcsec
 $I_{\text{xx}} \sim 0.12 \text{ arcsec}^2$

Gaussian w/ FWHM ~0.19 arcsec
 $I_{\text{xx}} \sim 0.0065 \text{ arcsec}^2$

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 $I_{\text{xx}} \sim 0.0065 \text{ arcsec}^2$

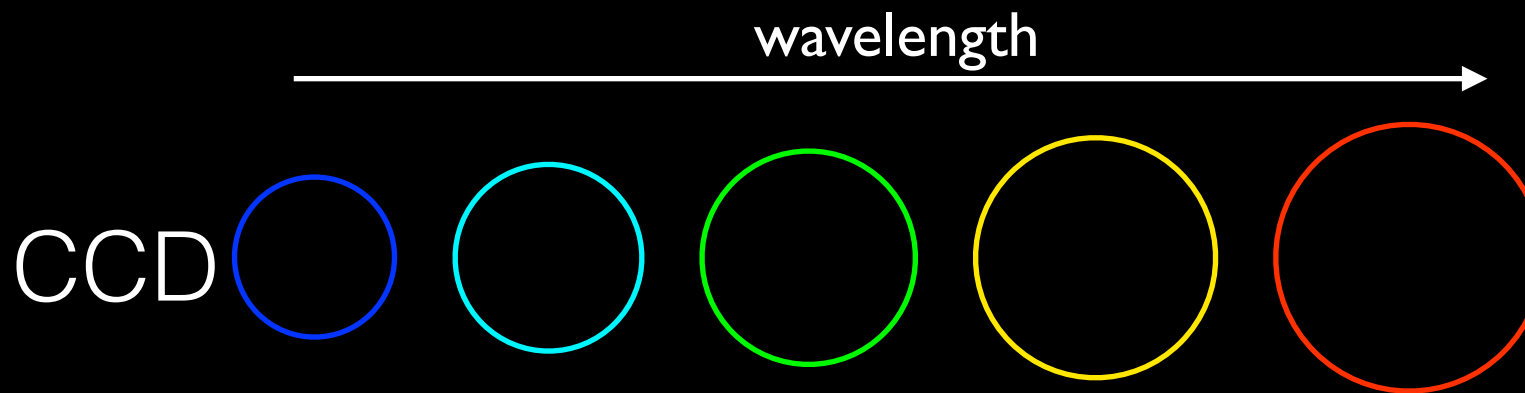
Compute “effective” PSF for a given spectrum/filter.

$$I_{\mu\nu}^{\text{PSF,eff}} = \frac{1}{\text{flux}} \int I_{\mu\nu}^{\text{PSF}}(\lambda) R(\lambda) S(\lambda) \lambda d\lambda$$

filter spectrum

Toy model — wavelength-dependent size

scope
+
atm



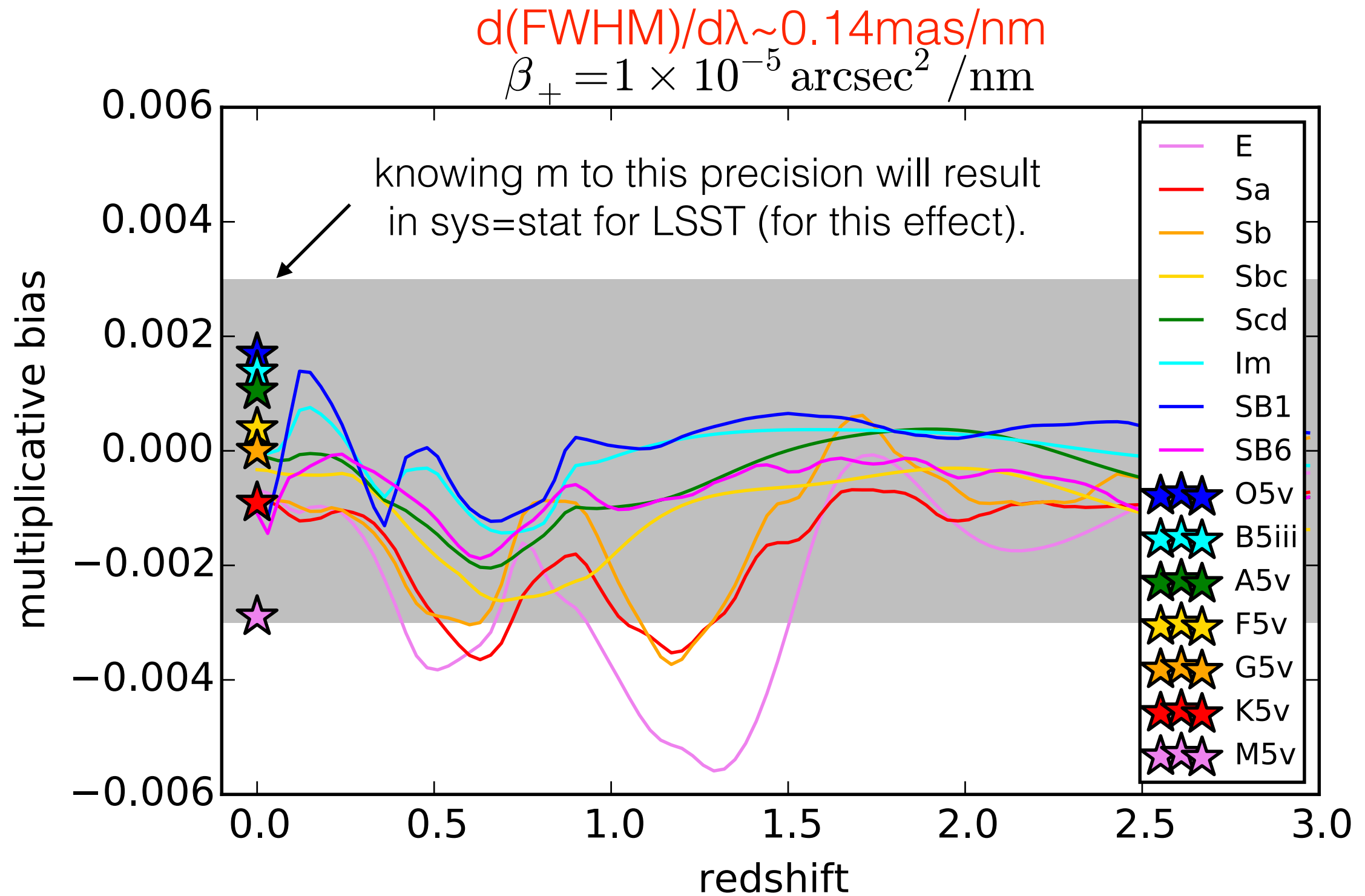
$$I_{xx}^{\text{PSF,CCD}}(\lambda) = I_{xx}^{\text{PSF,CCD}}(\lambda_0) + \beta_+ (\lambda - \lambda_0)$$

$$I_{yy}^{\text{PSF,CCD}}(\lambda) = I_{yy}^{\text{PSF,CCD}}(\lambda_0) + \beta_+ (\lambda - \lambda_0)$$

Set β_+ such that CCD PSF FWHM is 10% smaller at blue edge of r-band filter than at red edge.

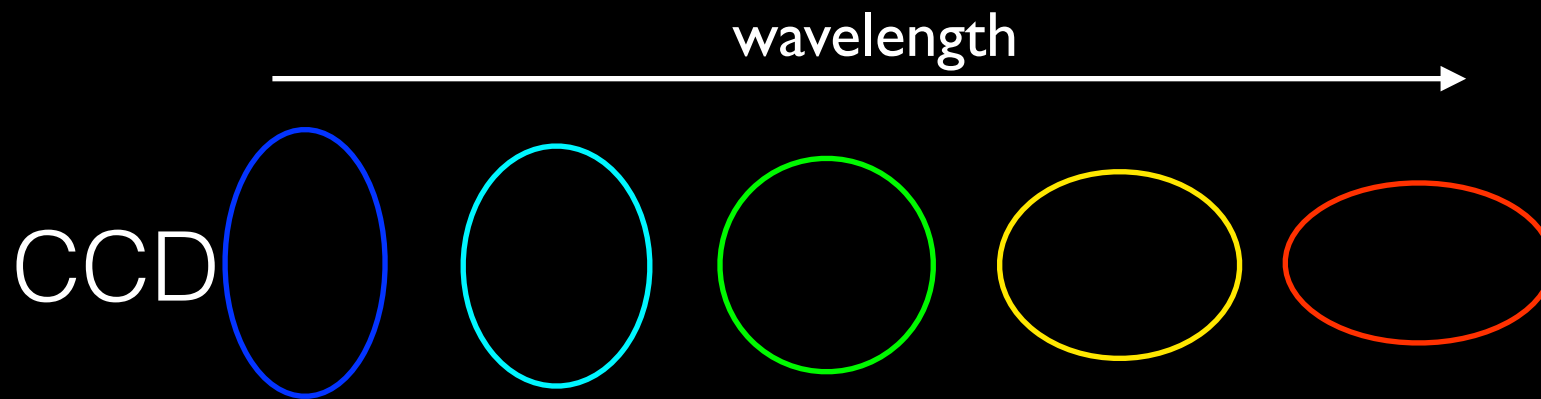
Works out to about 1×10^{-5} arcsec²/nm
or $d(\text{FWHM})/d\lambda \sim 0.14$ mas/nm

Toy model — wavelength-dependent size



Toy model — wavelength-dependent ellipticity

scope
+
atm



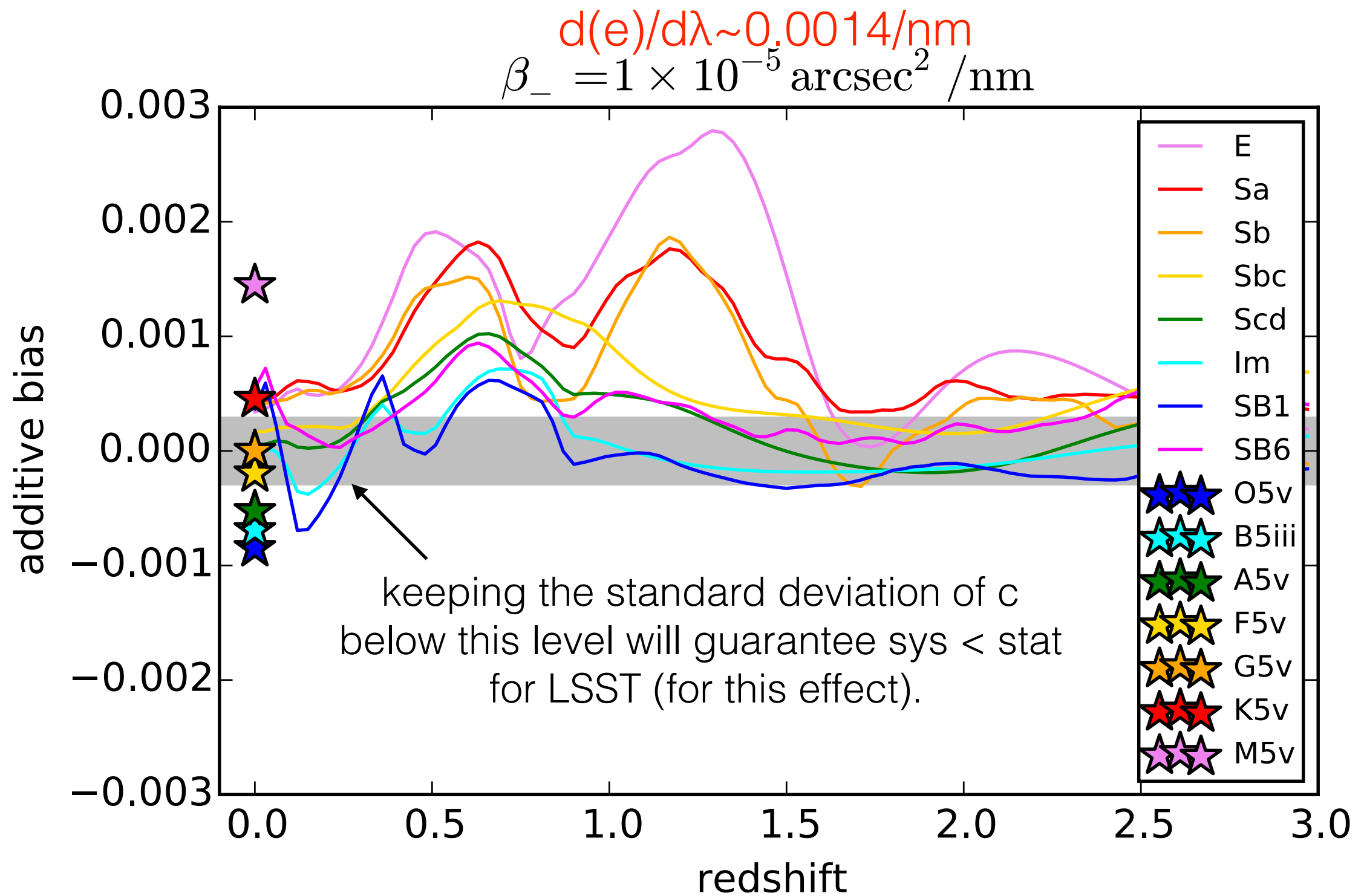
$$I_{xx}^{\text{PSF,CCD}}(\lambda) = I_{xx}^{\text{PSF,CCD}}(\lambda_0) + \beta_- (\lambda - \lambda_0)$$

$$I_{yy}^{\text{PSF,CCD}}(\lambda) = I_{yy}^{\text{PSF,CCD}}(\lambda_0) - \beta_- (\lambda - \lambda_0)$$

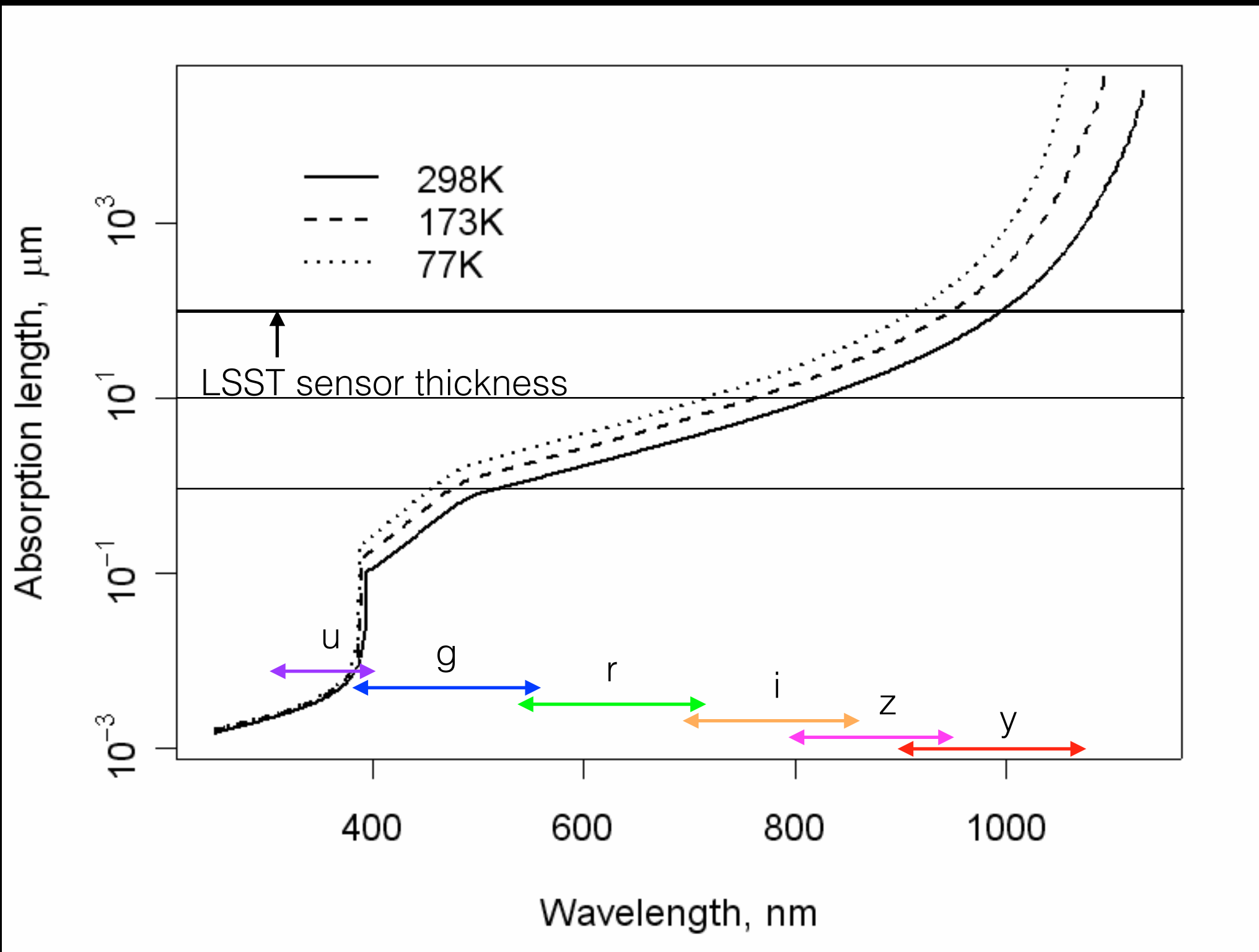
Set β_- such that CCD PSF ellipticity is -0.1 at blue edge
and +0.1 at red edge.

Works out to about 1×10^{-5} arcsec²/nm (same as before)
or $de_l/d\lambda \sim 0.0014$ / nm

Toy model — wavelength-dependent ellipticity



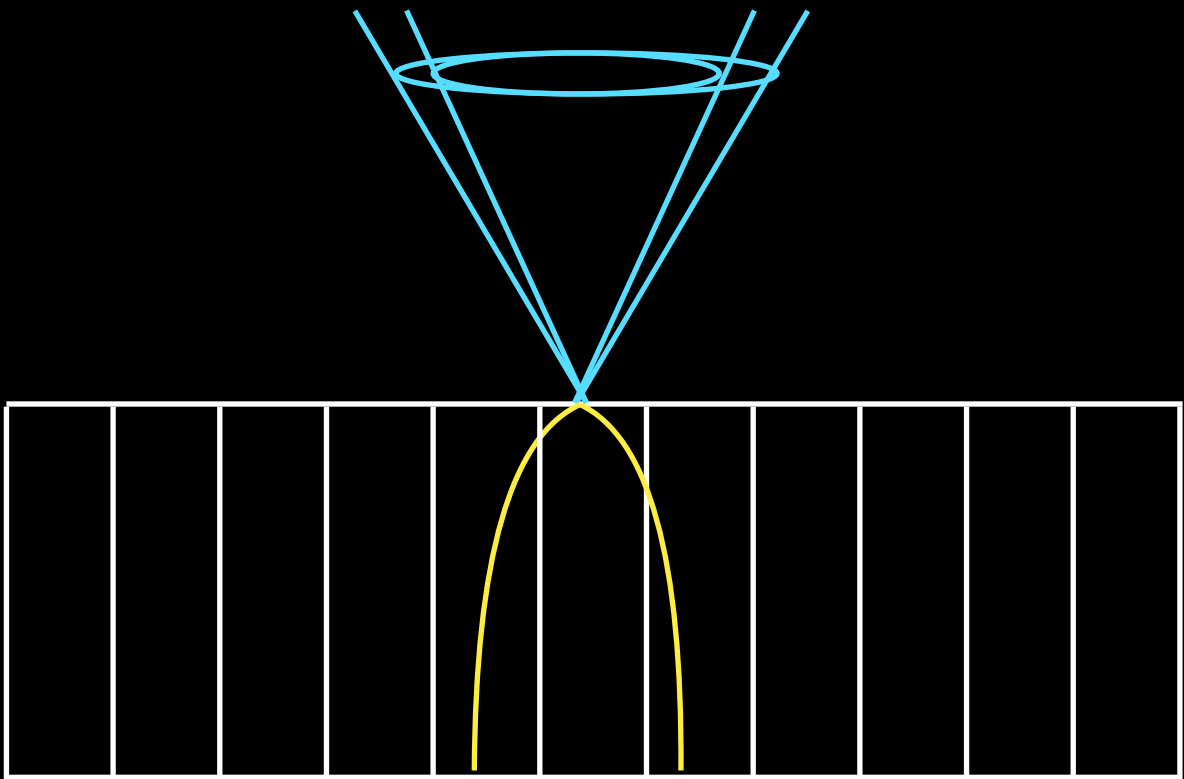
Source of CCD chromaticity



O'Connor++06

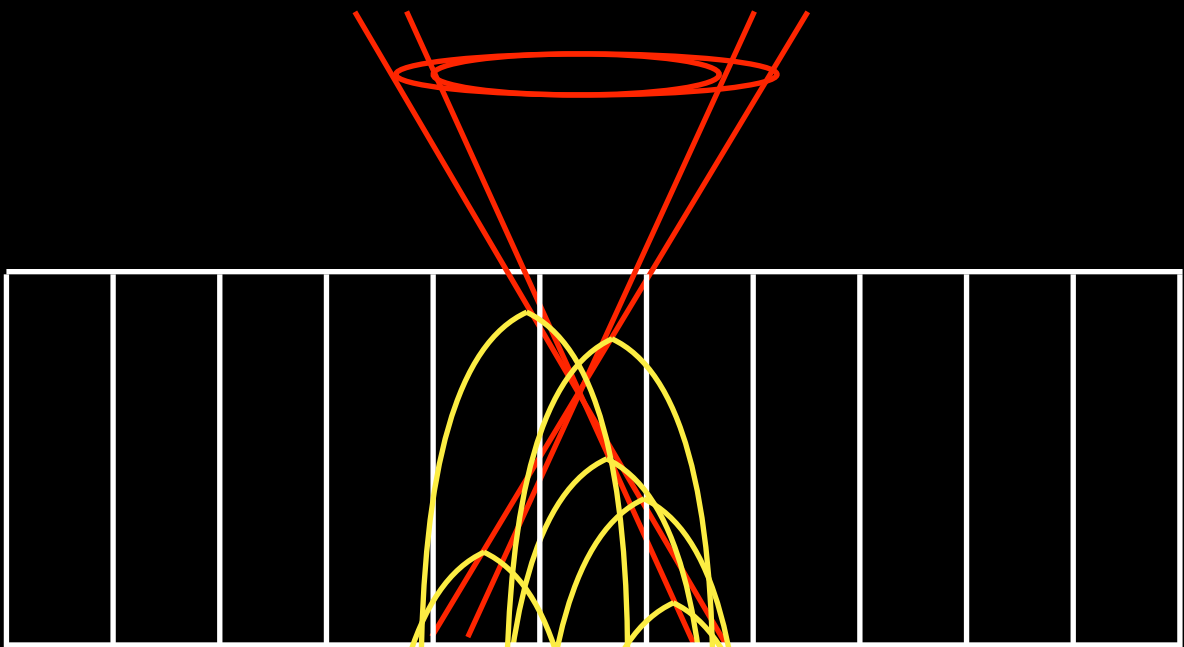
Spread in projected photo-conversion location

Blue photons
convert immediately



cartoon
for blue filter

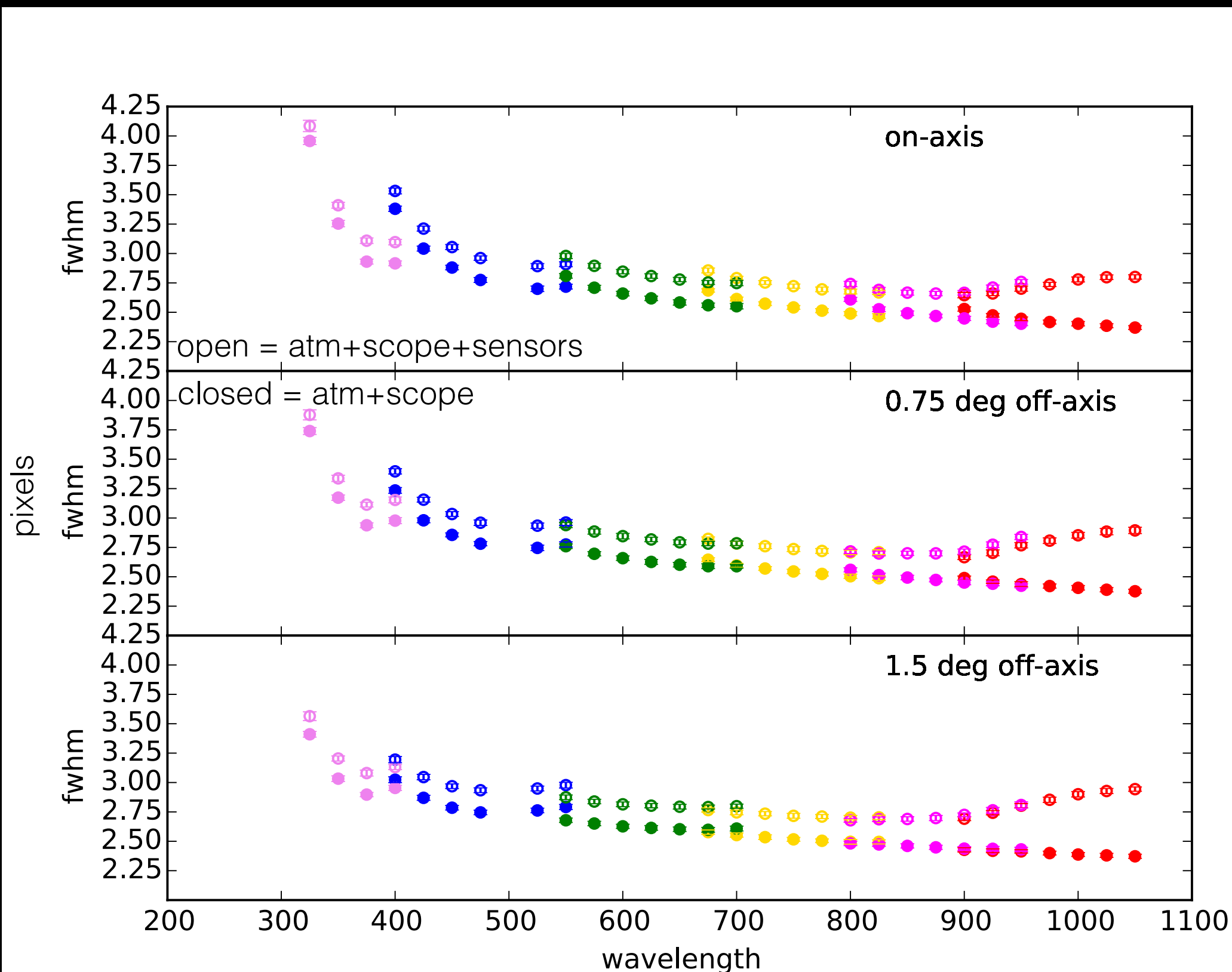
Redder photons
convert further
into the Silicon



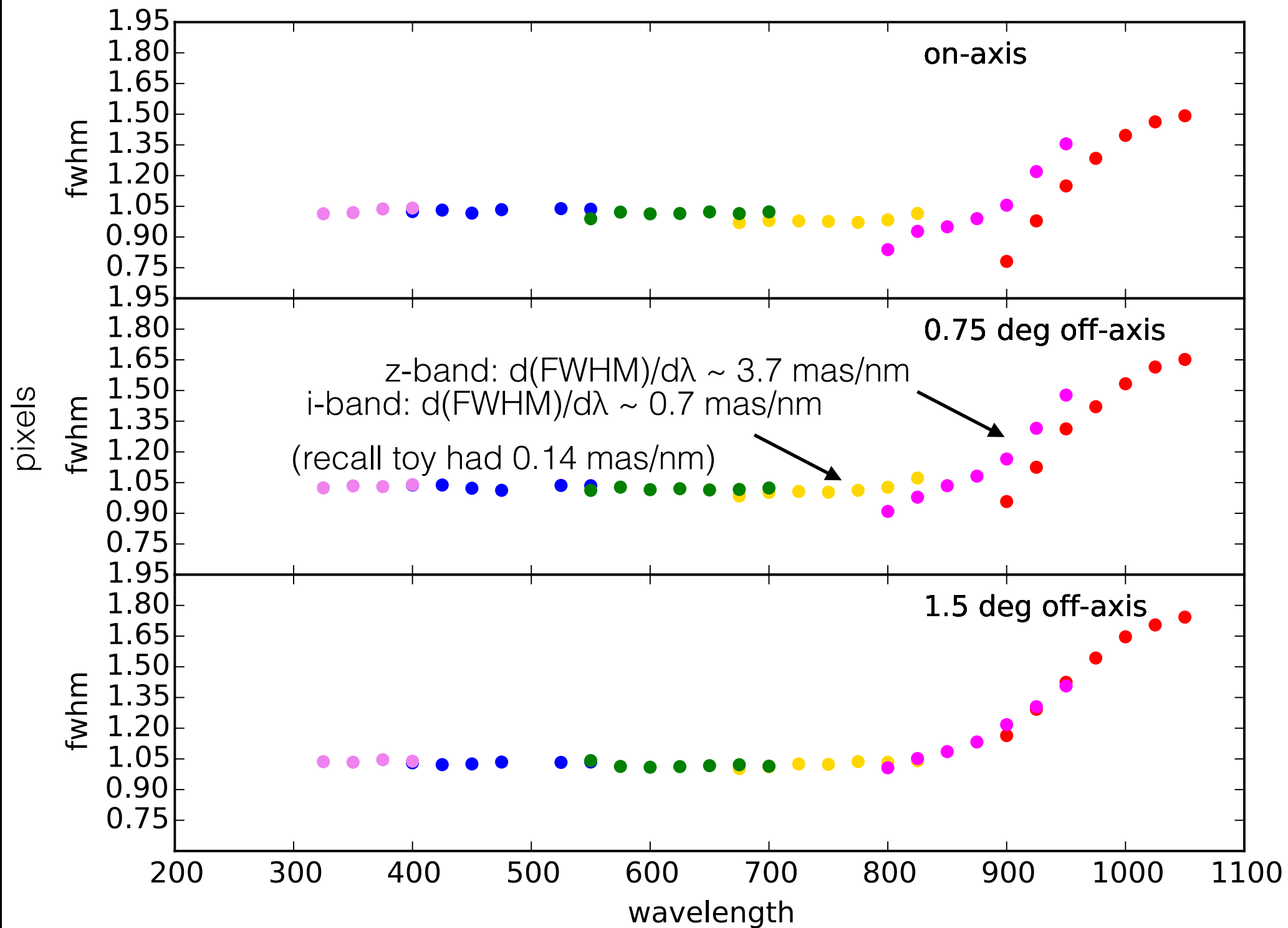
cartoon
for red filter
(ignoring refractive
index of silicon)

Phosim: PSF size (with and without sensor)

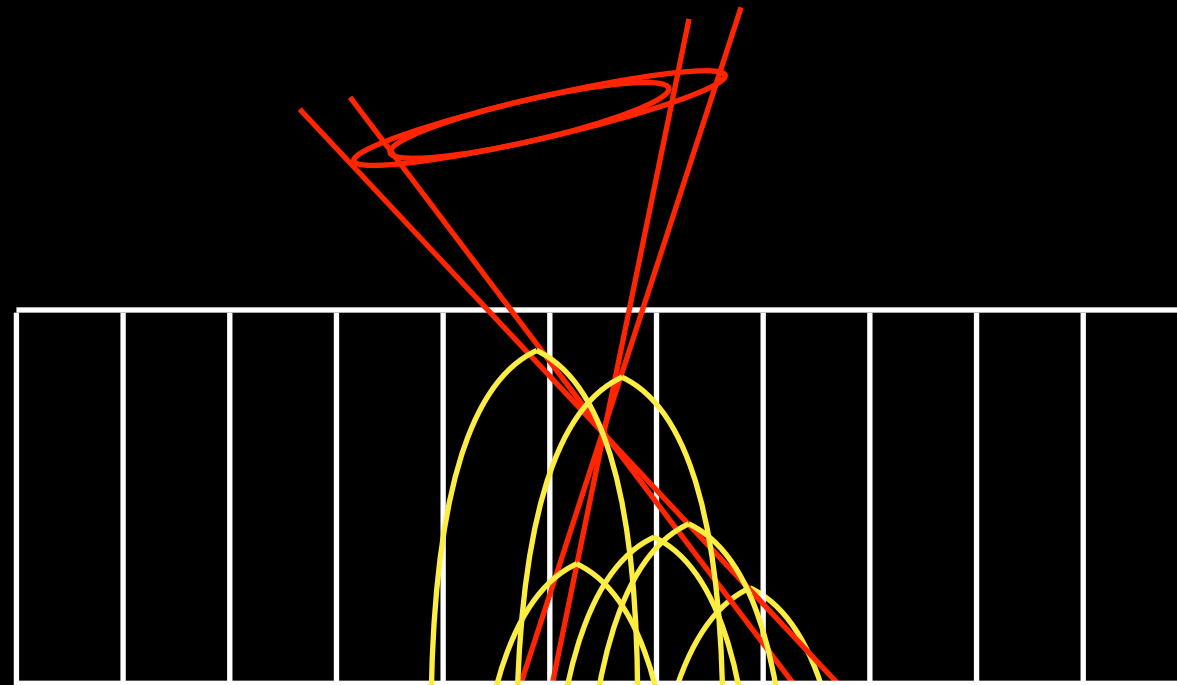
Use grid of monochromatic stars



Phosim: PSF size (sensor contribution only)



Ellipticity increases at edge of field as beam tilts.

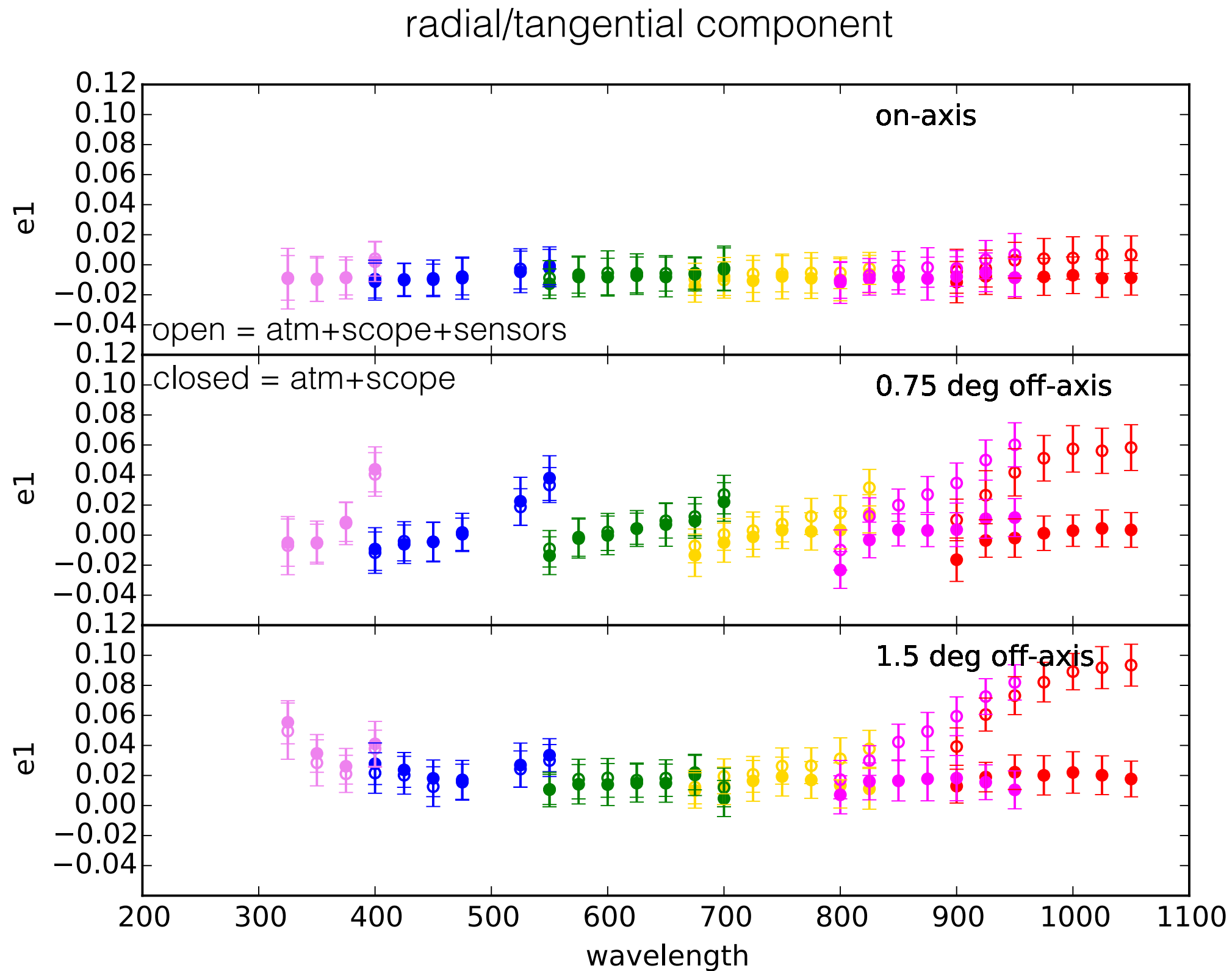


cartoon
off-axis
beam

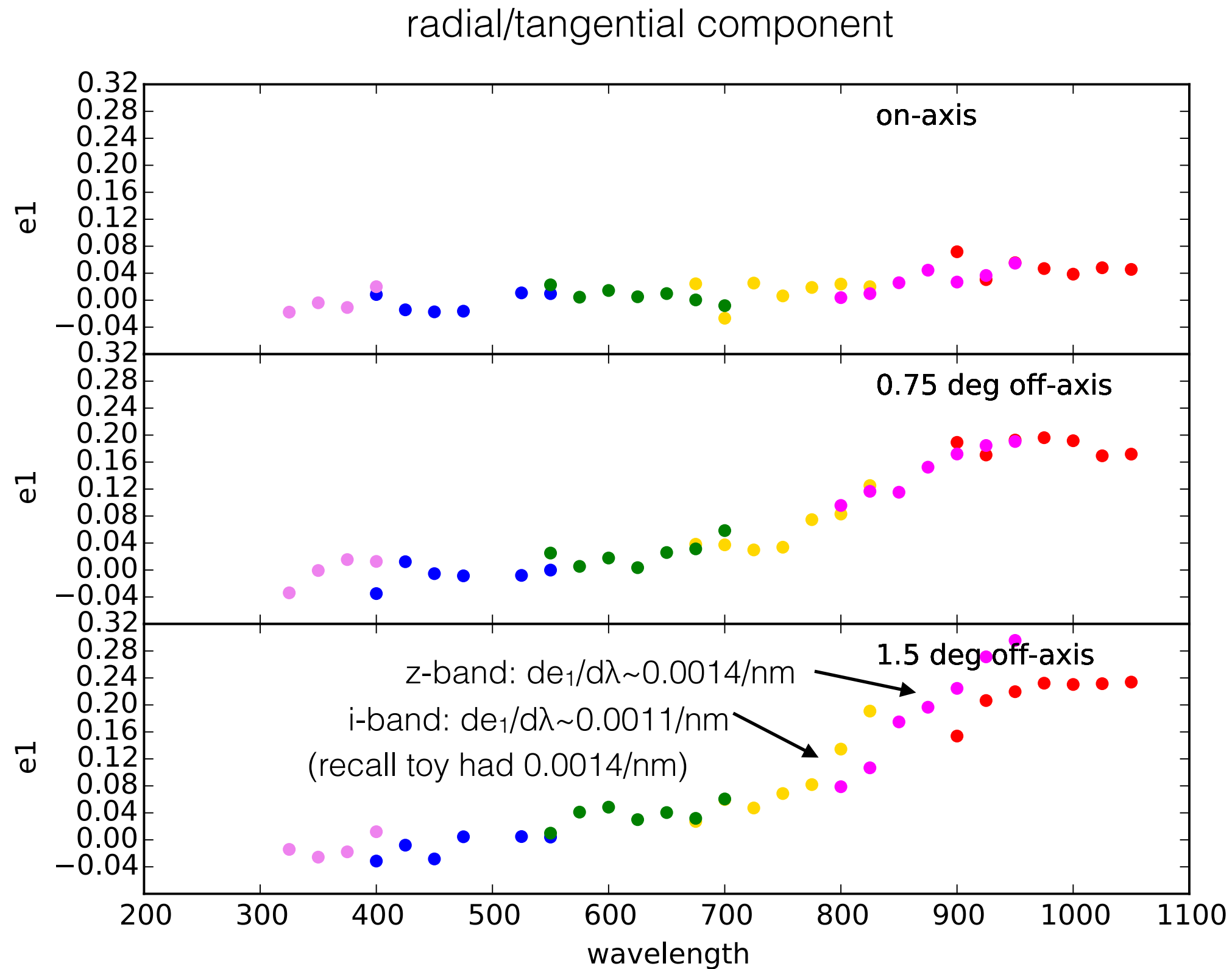
(ignoring refractive
index of silicon)

Also, reflections off front-side

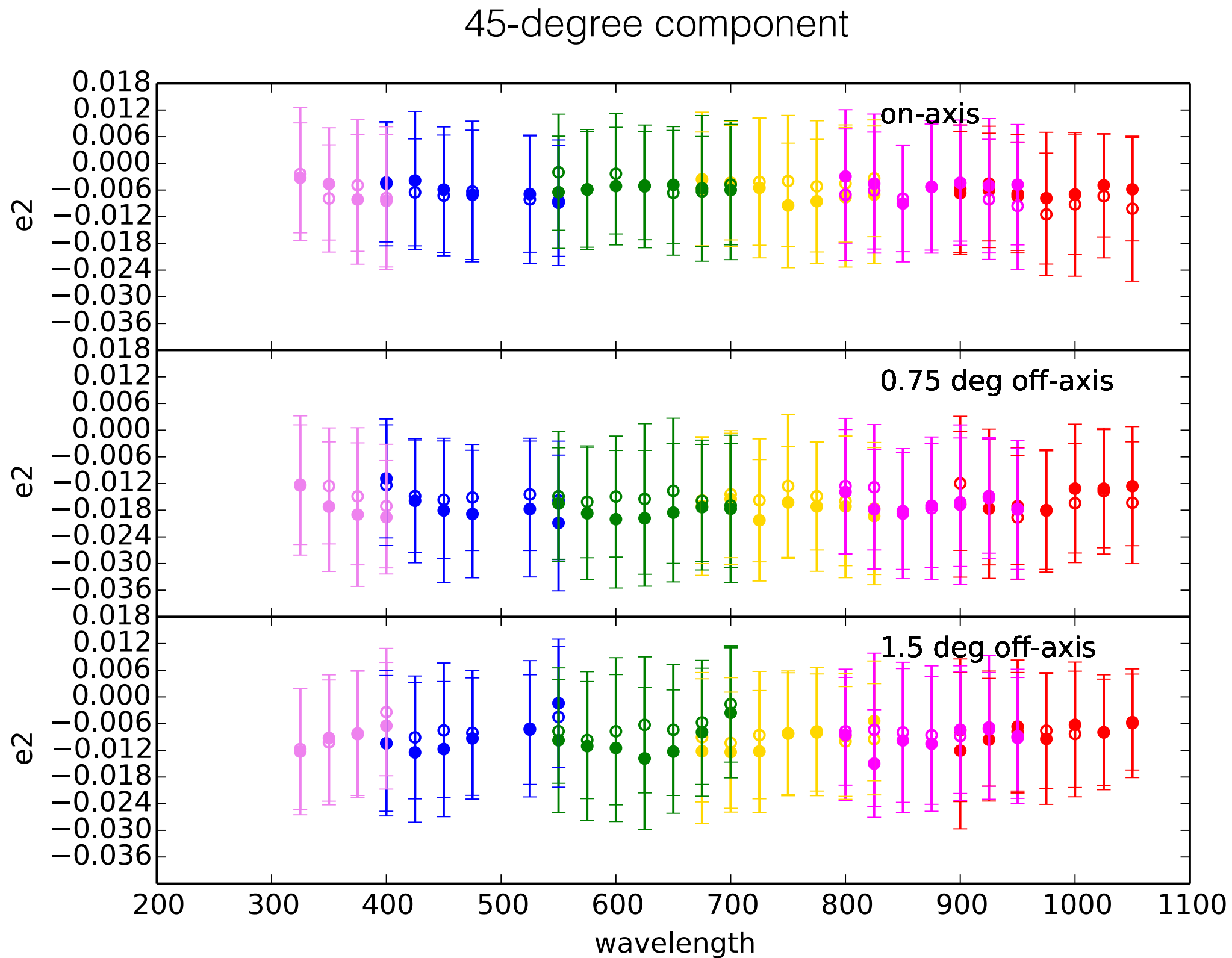
Phosim: PSF ellipticity (with and without sensor)



Phosim: PSF ellipticity (sensor contribution only)



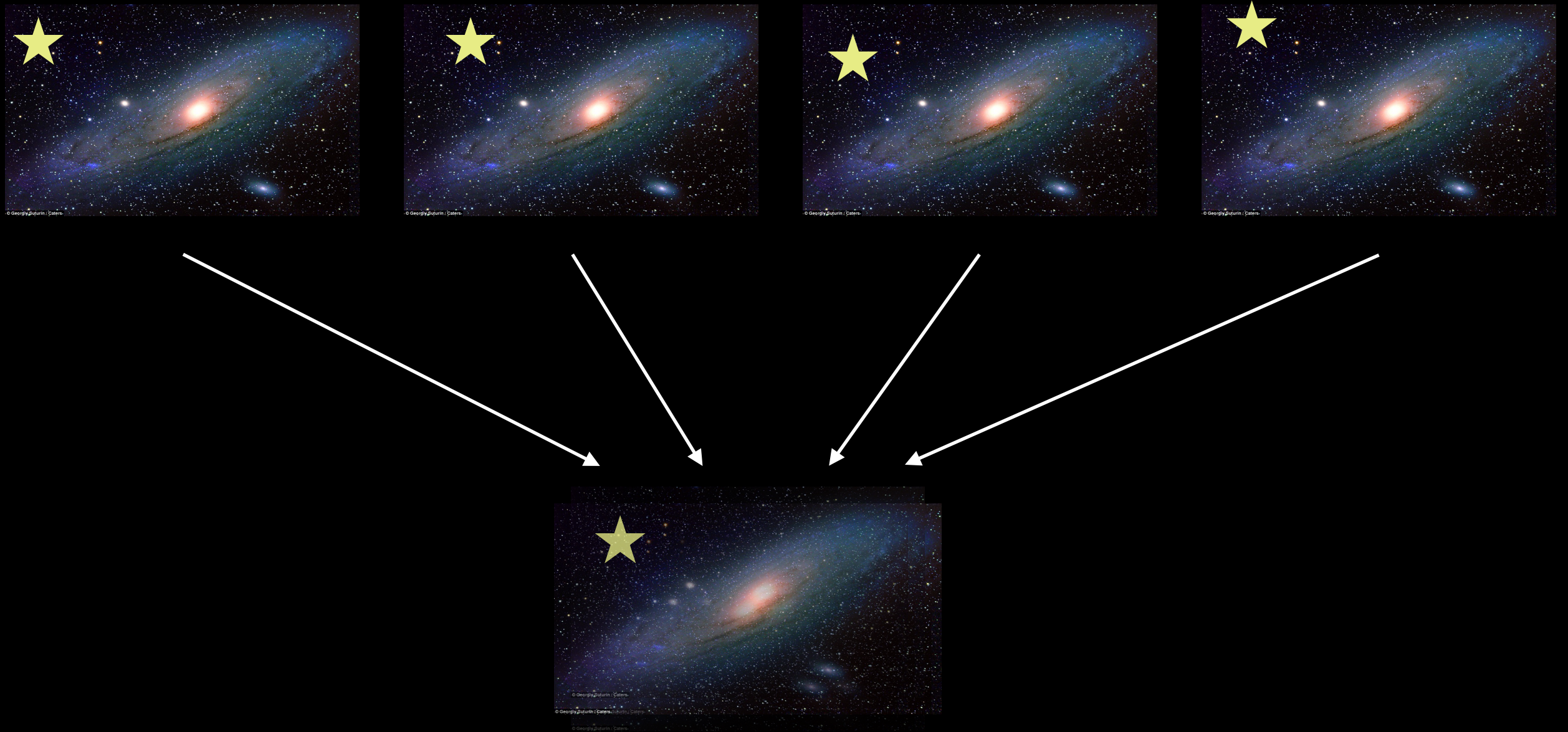
Phosim: sensor PSF ellipticity - no 45 degree component.



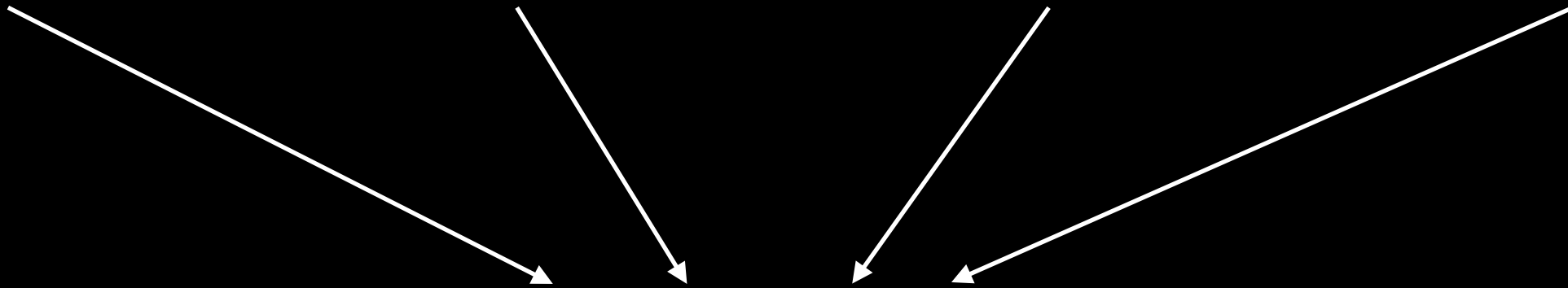
Misregistration bias - First moments matter too!



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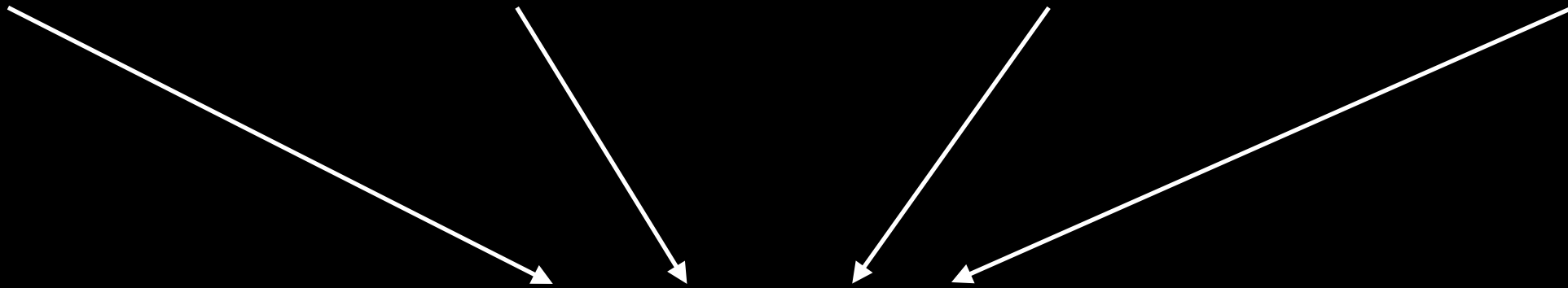
Misregistration bias - First moments matter too!



Fluctuations in the relative astrometry of stars and galaxies leads to blurred stacked galaxy image.



Misregistration bias - First moments matter too!



Fluctuations in the relative astrometry of stars and galaxies leads to blurred stacked galaxy image.



(Chromatic) tree-rings and/or (chromatic) edge roll-off may lead to misregistration.

Second moments of stacked galaxy image.

Assuming flux is the same in each epoch:

$$I_{\mu\nu}^{\text{stack}} = I_{\mu\nu}^{\text{single epoch}} + \underbrace{\langle (\mu - \bar{\mu})(\nu - \bar{\nu}) \rangle_{\text{epochs}}}$$

Since this term enters in exactly the same way as the PSF,

$$I_{\mu\nu}^{\text{obs}} = I_{\mu\nu}^{\text{gal}} + I_{\mu\nu}^{\text{PSF}}$$

it can be treated as an error in the PSF:

$$\Delta I_{\mu\nu}^{\text{PSF}} = \langle (\mu - \bar{\mu})(\nu - \bar{\nu}) \rangle_{\text{epochs}}$$

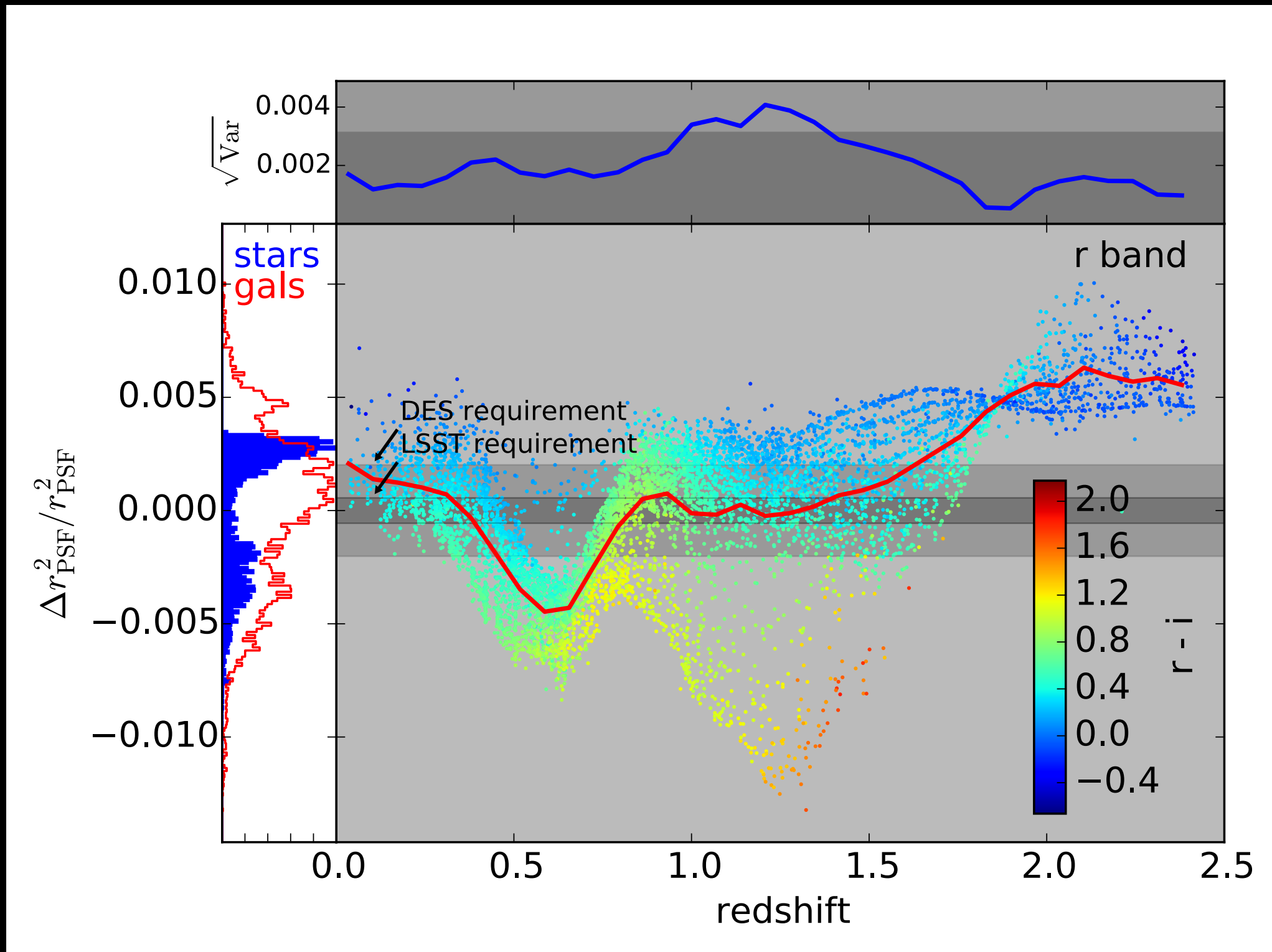
Implies the requirement:

$$\sqrt{\langle (\vec{x}_i - \langle \vec{x} \rangle)^2 \rangle} < 16 \text{ mas}$$

Corrections: learn SED from photometry

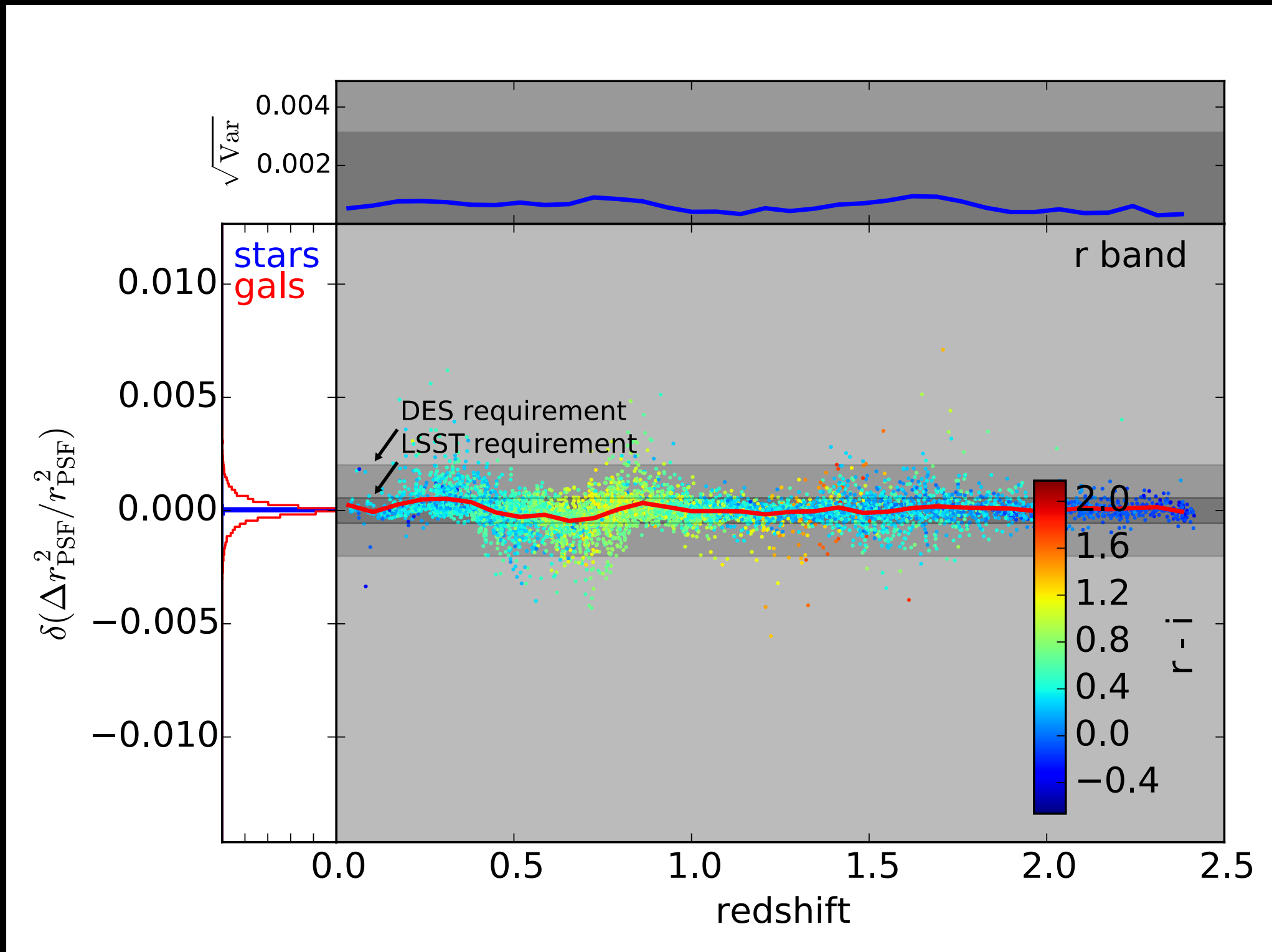
- Can correct if you know
 - $\text{PSF}(\lambda)$
 - The SED
- Train a machine-learning algorithm to predict chromatic bias as a function of photometry.
- Conceptually similar to a photometric redshift.

Corrections: learn SED from photometry



Meyers+Burchat2014 ([arXiv:1409.6273](https://arxiv.org/abs/1409.6273))

Corrections: learn SED from photometry



Meyers+Burchat2014 ([arXiv:1409.6273](https://arxiv.org/abs/1409.6273))

Conclusions

- Chromaticity in sensors is probably smaller than in the atmosphere or the optics, but still should be accounted for.
- Some rough numbers for LSST sensors (when individual systematic uncertainties will rival statistical uncertainties):
 - Uncertainty in $d(\text{FWHM})/d\lambda$ to $\sim 0.1 \text{ mas/nm}$
 - Uncertainty in $d(e)/d\lambda$ to $\sim 0.001/\text{nm}$
 - Individual exposure RMS astrometric shifts $\sim 16 \text{ mas}$.